



1 15 October 2021
2 EMA/CVMP/SWP/735418/2012 Rev.1*
3 Committee for Medicinal Products for Veterinary Use (CVMP)

4 **Guideline on determination of withdrawal periods for milk**
5 **Draft**

Draft agreed by Safety Working Party (SWP-V)	30 September 2021
Adopted by CVMP for release for consultation	7 October 2021
Start of public consultation	15 October 2021
End of consultation (deadline for comments)	17 December 2021

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9 This guideline replaces the Note for guidance for the determination of withdrawal periods for milk
10 (EMA/CVMP/473/98-FINAL).

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Keywords	<i>Withdrawal periods, milk, statistical approach</i>
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13 *The current revision consists of administrative changes made in order to align the guideline to the new
14 definitions and terminology provided by Article 4 of Regulation (EU) 2019/6. The references to the
15 legislation applicable and other scientific guidelines have also been updated.



16 **Guideline on determination of withdrawal periods for milk**

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49 **1. Introduction (background)**

50 For the establishment of withdrawal periods for milk different methods were available and used by
51 Member States. A harmonised method has been developed for decentralised applications for marketing
52 authorisations, as well as for centralised procedures, in order to facilitate that harmonised milk
53 withdrawal periods can be fixed in EU Member States.

54 The Note for Guidance Approach towards Harmonisation of Withdrawal Periods (EMEA/CVMP/036/95-
55 FINAL) [1] later replaced by the Guideline on determination of withdrawal periods for edible tissues
56 (EMA/CVMP/SWP/735325/2012) [21] provides detailed guidance on how to establish withdrawal periods
57 for edible tissues and was developed by the CVMP in order to provide a standardised approach within the
58 European Union. However, because the character of milk depletion data and the statistical aspects of
59 calculations with these data differ from those of meat residue data, a separate methodological approach
60 was necessary.

61 A harmonised method should fulfil the following criteria:

- 62 • It should provide safe withdrawal periods, derived from the depletion data in a scientifically justified
63 way.
- 64 • It should be applicable for most, if not all, realistic data sets, which meet certain reasonable and
65 feasible minimal criteria.
- 66 • It should enable Member States to establish equal withdrawal periods if depletion data are identical.
- 67 • Its use and application should be transparent
- 68 • The information necessary to apply the method should be made generally available.

69 The harmonised method for the determination of withdrawal periods for milk is the Time To Safe
70 Concentration (TTSC) method. With the TTSC method (fully described in 2.2) tolerance limits on the
71 number of milkings per animal - necessary for the residue concentration in the milk of most animals to
72 reach the safe concentration (most often the Maximum Residue Limit or MRL) - are calculated. The
73 described method is a modified version of a previously published method [2]. The harmonised method
74 assumes a log-normal distribution (of individual times to safe concentration), it corrects by monotonic
75 regression for increasing concentrations found during the depletion phase, and in a second monotonic
76 regression step it smoothes the relation between MRL (or other reference value)¹ and resulting
77 withdrawal period. In accordance with the position already taken with respect to the calculation of
78 withdrawal periods for meat [21], it is recommended to calculate the withdrawal period as the 95/95
79 tolerance limit, i.e. the upper 95% confidence limit of the 95th percentile of the population.

80 In a preliminary comparative study the method was found to be applicable in the largest number of
81 realistic cases and resulted in withdrawal periods comparable to (or slightly longer than) those resulting
82 from other tested methods (i.e. in cases where those methods were applicable). As the TTSC method is
83 also applicable if many concentrations are below the limit of quantification, if depletion is non-linear and
84 if variability is heterogeneous, it may be expected that it will be applicable for most data sets. Available
85 results showed that the assumption of log-normality and inclusion of monotonic regression in case of
86 increasing concentrations during depletion gave satisfactory results with most of the tested data sets.

87 The harmonised method laid down in this guideline is applicable to new products. It is recognised that
88 some data sets may not lend themselves to statistical analysis and, in accordance with the position
89 already taken with respect to the calculation of withdrawal periods for meat [21], in those cases a

¹ In the absence of a numerical MRL, another reference value may be used as the relevant limit for residue concentrations. This is applicable whenever "MRL" is mentioned further below.

90 statistical approach other than the harmonised method may be acceptable, but only on the condition that
91 the applicant provides data which adequately show that the proposed alternative is more appropriate
92 than the harmonised method. On these occasions it can be considered appropriate to extend the
93 calculated withdrawal period with an additional safety factor.

94 **2. Harmonised method for the determination of withdrawal** 95 **periods for milk in the European Union**

96 **2.1. Definitions and basic principles**

97 **2.1.1. Definition of "withdrawal period for milk"**

98 The definition given in Regulation (EU) 2019/6 [3] shall apply: " 'withdrawal period' means the minimum
99 period between the last administration of a veterinary medicinal product to an animal and the production
100 of foodstuffs from that animal which under normal conditions of use is necessary to ensure that such
101 foodstuffs do not contain residues in quantities harmful to public health ". It should be noted, that the
102 relevant value for the determination of withdrawal periods will be most often the MRL. However, for
103 substances without a MRL the relevant safe concentration might be based on an ADI or other scientifically
104 justified health based guidance value.

105 For example, a milk withdrawal period of 108 hours means that all the milk up to and including the last
106 milking before 108 hours after treatment must be discarded. Depending on the time of treatment in a 12-
107 hours milking cycle the last milk to be discarded may be from the milking at any time point at or after 96
108 hours after treatment but earlier than 108 hours after treatment. In this example milk from the first
109 milking at or after 108 hours is considered safe. Similarly, a milk withdrawal period of 12 hours means
110 that all milkings within a 12 hour period from the last treatment must be discarded and only milk taken
111 at or after 12 hours is considered safe.

112 **2.1.2. Milking interval in the experiment, and unit in which the withdrawal** 113 **period for milk should be expressed**

114 The withdrawal period for milk is initially calculated in milkings and rounded up to the first higher full
115 number of milkings. Since the predominant milking scheme is twice a day, experiments for the
116 determination of withdrawal periods for milk should be carried out with animals milked twice a day. For
117 reasons of consistency, between milking intervals of 12 hours are to be preferred. However, because a
118 different milking frequency can be used in practice, the final unit of the milk withdrawal period should be
119 real time. For this reason, the final withdrawal period is rounded up to multiples of 12 hours or whole
120 days and expressed in hours or days, respectively. If there are indications that this procedure does not
121 provide appropriate withdrawal periods for animals milked according to other milking schemes, data from
122 residue experiments with animals milked according to such other schemes might be of interest.

123 **2.1.3. Sampling protocol**

124 Withdrawal periods in the European Union, for all milk producing species, are established for individual
125 animals and not for tank milk because milk from individual or few animals is used for consumption and
126 for small-scale production of dairy products on farm level. Furthermore, too many assumptions are
127 needed to calculate withdrawal periods for tank milk: the number of animals and the fraction of treated
128 animals is variable and therefore assumptions of fixed numbers of animals introduce risks of
129 underestimating withdrawal periods.

130 In accordance with VICH GL 48 [5], four-quarter composite samples should be collected from individual
131 cows at each time point. For multiple doses products, samples should be taken after the last treatment,
132 for products that may qualify for a 0-day milk discard time, samples should also be collected during
133 treatment.

134 **2.1.4. Tolerance vs. prediction limits**

135 A tolerance limit gives 100q % confidence that at least 100p % of the individuals in a population is below
136 that limit. At the prediction limit we expect that 100p % of the individuals in a population is below that
137 limit. Consequently 95 % tolerance limits give more protection against incorrect results than 95 %
138 prediction limits. It has been claimed that 99 % prediction limits would give similar results as 95 %
139 tolerance limits [6], but this result has no general validity, and Chester et al. [2] noted that with the
140 TTSC approach the 99 % prediction limit consistently did not maintain its designed characteristics. It has
141 also been shown that prediction limits behave very strangely with severe extrapolation due to the
142 skewness of the underlying coverage distribution [7]. Based on these findings it is concluded that
143 tolerance limits are preferable to prediction limits.

144 **2.1.5. 95 % vs 99 % tolerance limits**

145 The EMA/CVMP approach [21] for tissue has adopted 95 % tolerance limits (with 95 % confidence level).
146 The choice between 95 % and 99 % tolerance limits should first of all be made by the responsible
147 authorities based on risk management decisions. Nevertheless, the following statistical truth should be
148 borne in mind: the higher the chosen percentile, the more statistical units (animals) will be needed in
149 experiments to establish a withdrawal period with sufficient accuracy. In general, samples from a
150 population allow better inference for statistics concerning the central part of the distribution (e.g. median,
151 quartiles, 95 % percentiles) than for statistics in the tails of the distribution (e.g. 99 % percentiles).

152 **2.1.6. Parametric vs. non-parametric tolerance limits**

153 Ideally an approach for establishing withdrawal periods should make as few as possible statistical
154 assumptions. In the approaches described in Annex I of this guideline the form of the statistical
155 distribution is assumed to be known: log-normal for concentrations in the SCLR (Safe Concentration-
156 Linear Regression) and SCPM (Safe Concentration Per Milking) approaches, and log-normal, normal or
157 Weibull in the respective variations of the TTSC approach. Especially in the TTSC case there is no
158 underlying theory which predicts the type of distribution: the choice made is empirical (over many data
159 sets; data sets are too small to allow a separate choice for each data set). This prompts the question
160 whether it would not be preferable to apply non-parametric (also called distribution-free) methods. Of
161 course, not to use a distributional assumption when actually it is true, will lead to loss of power, and
162 therefore longer withdrawal periods.

163 Non-parametric tolerance limits are based on order statistics, which means that the tolerance limit is just
164 one of the original observations in the sample (e.g. the highest, or the next-highest observation). Non-
165 parametric tolerance limits are not exact, because a choice has to be made from a finite set of values.
166 Conservative non-parametric 100p % tolerance limits provide a confidence level of at least 100q %. This
167 can only be achieved for a certain minimal sample size, which can be calculated as $n \geq \ln(1-q) / \ln(p)$
168 (see e.g. [9], p. 93). Therefore, with confidence level $q=0.95$, we will need at least 59 observations
169 (animals) for a 95 % non-parametric tolerance limit, and no less than 299 observations (animals) for a
170 99 % non-parametric tolerance limit. It is clear that the number of animals that can be included in
171 depletion experiments in practice will be too small to use non-parametric methods, and therefore one has
172 to rely on the distributional assumptions of parametric methods.

173 **2.1.7. Selection of animals in experiments**

174 From a statistical perspective, a sample size $n = 20$ is the very minimum to allow empirical estimates of a
175 95 % percentile. A smaller sample size (i.e. number of animals) amounts to the use of extrapolation in
176 the coverage. A sample size larger than 20 is advisable to give the desired confidence level (95 %) at
177 least some empirical basis ($n=59$ would be necessary to allow a completely non-parametric approach,
178 see 2.1.6).

179 With respect to stratification, it has been suggested to include both high yielding cattle at an early stage
180 of lactation, and low yielding cattle at a late stage of lactation in a residue depletion study. This should
181 guarantee that at least some of the between animal variability is included in the study. However, this is
182 only a partial solution to the problem of how to take inter animal variability into account since, for
183 instance, differences in races or food regimes may be important as stratifying factors, too. Therefore, it
184 seems best not to prescribe stratification, but only to require a representative sample from the relevant
185 population of animals. Selection of animals should be made with attention for at least those factors,
186 which are known to be important, such as milk yield. In a representative sample the inter animal
187 variability will be an honest estimate of the inter animal variability in the population. The inter animal
188 variability in the study now is artificial; therefore the 95 % percentile, which is central in the statistical
189 approach, now refers to an artificial population of animals. In principle, this can be corrected, if the true
190 proportion of high/low yielding animals in the complete population of cows would be known.

191 Therefore, a sufficient number of animals (minimum number: $n = 20$) should be sampled. It is important
192 that also a representative sample of animals should be taken from the relevant target population (i.e. the
193 distribution of milk yields should be realistic, the animals should be kept under normal zootechnical
194 conditions).

195 The principles mentioned in VICH GL 48 should be followed.

196 **2.1.8. Time of last administration**

197 A withdrawal period is actually a discrete variable. The milk from two subsequent milkings may be unsafe
198 and safe, respectively, and it is not sensible to define safety at intermediate time points. It is
199 recommended that, in depletion studies, the last administration of the compound shall be 12 hours (one
200 milking period) before milking 1. If this condition is not met, the data from milking 1 should be discarded,
201 because there is no suitable model or data for within milking cycle kinetics. In general, milk collected in a
202 12 hours milking scheme, but less than 12 hours after treatment will be a mixture from the periods
203 before and after treatment, and may therefore have a lower concentration than milk collected 12 hours
204 after treatment. Consequently, the lowest possible withdrawal period for general use is the time of the
205 first milking at or after one full milking period.

206 **2.1.9. Shortest possible withdrawal period**

207 In some cases all milk residue concentrations may be below or at the MRL^1 from the first milking after
208 treatment on. In this case the harmonised TTSC method cannot be used (because there is no variability
209 in times to safe concentration). If a sufficiently large proportion of the concentrations is between the LOQ
210 and MRL^1 the data might still be processed statistically, e.g. by calculation of the tolerance limit for the
211 first milking (see annex 1: SCPM method). If a withdrawal period of 1 milking results from an experiment
212 with an interval of 12 hours between the treatment and the first milking, the withdrawal period should
213 thus be 12 hours. If most or all residue concentrations are below the LOQ, no meaningful calculation of a
214 95/95 tolerance limit is possible (unless $n \geq 59$, see 2.1.6), and, provided that the LOQ is sufficiently below
215 or equal to the MRL^1 , it is acceptable to establish a withdrawal period of 12 hours.

216 Note that a withdrawal period of 12 hours means that no milk at all has to be discarded if a single
217 treatment is given just after a milking and 12 hours before the next milking. However, in a setting where
218 usual milking is more frequent (e.g. 3 times per day, or at the animal's choice by a milk robot), milking
219 during the first 12 hours should be avoided or the milk discarded.

220 The only way to obtain withdrawal periods shorter than the standard milking interval (12 hours) is to
221 conduct residue experiments with a shorter interval between 0th milking/last treatment and first milking.

222 **2.1.10. Withdrawal periods for intramammary products**

223 In experiments for the establishment of withdrawal periods for products intended for intramammary
224 treatment at drying off, all quarters should be treated, i.e. normally four quarters in bovine. Although, in
225 practice, it is unlikely that all quarters will be treated with a product for intramammary treatment during
226 lactation at the same time, this should however be done in a residue study to represent a worst case
227 situation.

228 For products intended for intramammary treatment at drying off, the principles laid down in this note for
229 guidance are applicable. Statistical methods should be applied on the residue concentrations found in the
230 milk after birth. However, the variation in the length of the dry period may cause a large variability
231 between animals. Therefore, the experiment should be designed in such a way that a sufficient number of
232 animals give birth in a limited time interval. For instance, if an applicant wishes to establish a withdrawal
233 period for cows calving 30 days after treatment, data are needed from at least 20 cows calving between
234 e.g. 20 and 30 days after treatment. However, if the applicant wishes to establish a withdrawal period for
235 animals calving after the more common dry period of 60 days, data are needed from at least 20 cows
236 calving before 60 days after administration, e.g. between 40 and 60 days after treatment.

237 The applicant should try to keep the differences between dry periods between animals within the
238 experiment as small as possible, in order to keep the variability as small as possible. This can, for
239 instance, be done by drying-off and infusing animals with the formulation when they are at the targeted
240 number of days from the expected date of giving birth, provided that appropriate consideration is given
241 to animal welfare issues.

242 Since the differences in residue concentrations between animals which differ little in length of dry period
243 are often in the same order of magnitude as the relatively large differences found already between
244 animals with equal dry periods, differences between animals with slightly differing length of dry period
245 may not add too much to the large inter-individual differences which are unavoidable anyway. A number
246 of data sets are currently being evaluated in order to reconsider a new statistical approach when dealing
247 with animals that have different lengths of dry period.

248 **2.2. Full description of the Time-To-Safe-Concentration (TTSC) method**

249 The Time-To-Safe-Concentration (TTSC) method calculates a tolerance limit on the number of milkings
250 per animal. This tolerance limit is the time necessary for the residue concentration in the milk of most
251 animals to reach the safe concentration (most often the MRL¹). The method assumes a log-normal
252 distribution (of individual times to safe concentration), it corrects by monotonic regression for increasing
253 concentrations found during the depletion phase, and in a second monotonic regression step it smoothes
254 the relation between MRL¹ and resulting withdrawal period. The withdrawal period is calculated as the
255 95/95 tolerance limit, i.e. the upper 95% confidence limit of the 95th percentile of the population of
256 individual times to safe concentration. This section gives a full stepwise description of the calculations of
257 the method.

258 For the purpose of statistical analysis, true milk withdrawal period is interpreted here as the time period
259 from the time of last administration to the time point at and where after 95 % of the population of

260 interest has residue levels not higher than the MRL¹ The population of interest is taken to be all individual
261 animals, which could potentially be treated with the medicinal product.

262 In general the true milk withdrawal period is unknown. It has therefore to be estimated from empirical
263 data from representative treated animals. The estimated milk withdrawal period (*WP*) is chosen such that
264 there is at least 95 % confidence (under the model assumptions) that the true withdrawal period is not
265 higher than the estimated withdrawal period. Such estimators are known as tolerance limits. A theoretical
266 comparison with other type of estimators (prediction limits, expected percentiles) has been made for the
267 tissue case, and is available on request [7].

268 The described approach is a modification and extension of the method described in [2]. In its simplest
269 form one takes, for each animal, the first time point where the measured concentration is at or below the
270 MRL¹, and stays below the MRL¹ at later times. This time point is labelled the time-to-safe-concentration
271 (*TTSC*). With replicate measurements on each milk sample geometric mean concentrations are used in
272 this step. The resulting set of *TTSC* points is then used to calculate a tolerance limit. A critical issue with
273 this method is the choice of distributional assumption for the *TTSC* points. Chester et al. [2] assume a
274 normal distribution. In the harmonised method described here *TTSC* points are assumed to arise from a
275 log-normal distribution, which has been shown to be a better fit for a number of real data sets from
276 industrial practice (see Annex I.5.3.1).

277 The method contains a pre-processing step in which monotonic regression is applied to the log
278 concentration data versus time. This least squares procedure replaces the data values of each animal by
279 fitted values under the only condition that these fitted values should be non-increasing with time. This
280 step incorporates the prior knowledge that during the depletion period residue concentrations are
281 decreasing. This pre-processing step removes the influence of variability due to incidental increases in
282 measured values during the depletion phase.

283 The method also contains a post-processing step in which monotonic regression is applied to preliminary
284 estimates of withdrawal period as a function of the MRL¹ considered as a variable. Using one and the
285 same data set, it is reasonable to expect a longer (or equal) withdrawal period when the MRL¹ would be
286 lowered (and vice versa). However, due to statistical fluctuations, this is not guaranteed with the *TTSC*
287 method as described so far. Therefore, an additional monotonic regression is applied to obtain such a
288 relation.

289 The *TTSC* method consists of the steps described below. An example, using the calculations described in
290 this chapter, can be found in annex II. A computer program, assisting in the calculations laid down in this
291 guideline, is available at EMA homepage².

292 *Step 1. Notation and censoring indicator*

293 Data should be available for a representative sample of n animals, with $n \geq 20$. Suppose there are data
294 from J milkings per animal, and K replicated measurements on each milk sample (in practice, K will often
295 equal 1). Let c_{ijk} denote the k 'th measured concentration in a milk sample from animal i and milking j .

296 Some of the concentrations may be given as ' $<LIM$ ', where LIM is just the lower limit for reporting a
297 numerical value. In practice, the limit of quantification (LOQ) is often used. Also in this paper 'the LOQ ' is
298 used to denote the reporting limit, but we assume no statistical properties of the LOQ . MRL^1 denotes the
299 maximum residue limit for the marker residue.

300 In order to distinguish measured real values from results reported as 'below LOQ ' a censoring indicator
301 variable z is constructed as follows:

$$302 \quad z_{ijk} = 0 \quad \text{if } c_{ijk} \geq LOQ$$

² <https://www.ema.europa.eu/en/determination-withdrawal-periods-milk>

303 $z_{ijk} = 1$ if $c_{ijk} < LOQ$

304 Measured concentrations $c_{ijk} < LOQ$ are temporarily replaced by LOQ (this is for the data preprocessing in
305 steps 2 and 3 only). Note that values equal to LOQ may have $z_{ijk}=0$ or $z_{ijk}=1$ at this point.

306 *Step 2. Logarithmic transformation of concentrations and means of replicate measurements*

307 Natural logarithms of the concentrations are taken:

308 $y_{ijk} = \ln(c_{ijk})$

309 If there are $K > 1$ replicate measurements on any milk sample, y is averaged over the last index:

310 $y_{ij} = \sum_{k=1}^K y_{ijk} / K$

311 The geometric mean concentration of milk sample ij is

312 $c_{ij} = e^{y_{ij}}$

313 The censoring indicator for sample ij is

314 $z_{ij} = \min_k(z_{ijk})$

315 i.e. the measurement on milk sample ij is considered to be below the LOQ only if *all* measurements on
316 that sample are below the LOQ . If any measurement on this sample is uncensored, the conservative
317 (high) concentration estimate c_{ij} is used in the following as a real measurement.

318 *Step 3. Monotonic regression concentration vs. time*

319 For each animal i separately, a set of non-increasing log-concentration values is obtained by monotonic
320 regression. Monotonic regression does not change the data unless they are in the wrong order: during
321 the depletion phase we expect concentrations decreasing with time, therefore only concentrations at time
322 periods showing an increase with time will be changed. Basically, log-concentration values in the wrong
323 order (a high value following a low value) are replaced with their average. When more than two values
324 are out of order, new values can be found from an easy iterative algorithm. Start with weights $w_j=1$ for
325 all time points j . Then, for any adjacent pair $(j, j+1)$ with increasing concentration values ($y_{ij} < y_{i,j+1}$),
326 replace the pair by one value, the weighted average

327 $(w_j y_{ij} + w_{j+1} y_{i,j+1}) / (w_j + w_{j+1})$

328 and set the new weight equal to $w_j + w_{j+1}$. Repeat this procedure until the resulting averages per animal
329 do not show increases in concentration over time. The new averages then replace the values y_{ij} in the
330 following steps. Average values are valid for each of the underlying time points. For more information see
331 e.g. [10].

332 The censoring indicator z_{ij} is set to 0 if a value $y_{ij}=LOQ$ is replaced by a higher value in the monotonic
333 regression. This will happen when censored observations are followed by values above the LOQ .

334 *Step 4. Set values for graphical display of data below the limit of quantification*

335 For samples with $z_{ij}=1$, the concentrations c_{ij} are set to $\frac{1}{2}$ of the LOQ , and the log-concentrations y_{ij} to \ln
336 $(\frac{1}{2} LOQ)$. This is done for graphical purposes only, so that censored observations are shown in plots as
337 points below the LOQ line. This step has no influence on the estimation of the withdrawal period in steps
338 5-10.

339 *Step 5. Calculate times to safe concentration*

340 For each animal i identify the first time point t_j (in milkings) with $c_{ij} \leq MRL^1$ and $c_{ik} \leq MRL^1$ for all $k > j$. This
341 time point is labelled as the time-to-safe-concentration for animal i , and is denoted $TTSC_i$.

342 Note: if the last concentration in the data set is still above MRL^1 , $TTSC_i$ cannot be calculated. In that case
 343 the TTSC method is not applicable to the data set.

344 Step 6. Change to logarithmic scale

345 Calculate for each animal i the natural logarithm of the time to safe concentration:

346 $x_i = \ln(TTSC_i)$

347 Step 7. Tolerance limit calculation

348 The calculation is based on the assumption of a normal distribution for x . First calculate the mean and the
 349 standard deviation of the n values x_i :

350 $m = (1/n) \sum_{i=1}^n x_i$

351 $s_x = \{1/(n-1)\} \sum_{i=1}^n (x_i - m)^2$

352 Values x_i are from a discrete set (times of milking), whereas the tolerance calculations assume a
 353 continuous variable. To avoid zero standard deviations (when all x_i are equal) s_x is not allowed to become
 354 lower than a minimal value which represents the rounding error. The minimal standard deviation of x is
 355 approximately equal to the minimal coefficient of variation of $TTSC$ values: it is set to $(1/\sqrt{12}) / e^m$.

356 The tolerance limit is calculated as

357 $x_{tol} = m + k s_x$

358 where the tolerance limit factor k for a 95/95 tolerance limit and a specific value of n can be found in
 359 Table 1³.

Table 1. One-sided tolerance limit factors k for standard 95/95 tolerance limit calculations ($p=0.95$; $1-\alpha=0.95$). Data from [13], and calculated.

n	k	n	k
2	26.260	21	2.371
3	7.656	22	2.350
4	5.144	23	2.329
5	4.210	24	2.309
6	3.711	25	2.292
7	3.401	26	2.275
8	3.188	27	2.260
9	3.032	28	2.246
10	2.911	29	2.232
11	2.815	30	2.220
12	2.736		
13	2.670	40	2.126
14	2.614	50	2.065
15	2.566	60	2.022
16	2.523	70	1.990
17	2.486	80	1.965
18	2.453	90	1.944
19	2.423	100	1.927
20	2.396	∞	1.645

³ More generally k can be calculated as $k = t'_{n-1}(1-\alpha; \delta) / \sqrt{h}$, where $t'_{n-1}(1-\alpha; \delta)$ is the $100(1-\alpha)$ percentile of the non-central t distribution with $n-1$ degrees of freedom and non-centrality parameter $\delta = z_p \sqrt{h}$. In the latter expression z_p is the $100p^{\text{th}}$ percentile in the standard normal distribution (e.g. $z_{0.95}=1.645$). A standard reference for the non-central t distribution is [11]. Standard algorithms are available for calculating cumulative probabilities in the non-central t distribution, for example algorithm AS5 in the Applied Statistics collection available in STATLIB on the Internet, and described in [12]. Percentiles of the non-central t distribution can be calculated by applying a simple search algorithm to the algorithm of AS5, e.g. consisting of a fixed-step search plus a bisection search. Approximative formulas to calculate tolerance limits exist, see e.g. Guideline on determination of withdrawal periods for edible tissues (EMA/CVMP/SWP/735325/2012) [21]

360 *Step 8. Un-rounded withdrawal period*

361 The tolerance limit is converted to an un-rounded withdrawal period (*UWP*) at the ordinary time scale (in
362 milkings):

$$363 \quad UWP = e^{X_{tol}}$$

364 *Step 9. Monotonic regression on UWP vs. MRL¹ relation*

365 Calculations of step 5-8 are repeated for a range of *MRL¹* values. In principle, all *MRL¹* values in the range
366 of the data are investigated. In practice, it is sufficient to calculate *UWP* for the real *MRL¹*, and for *MRL¹*
367 values equal to all concentration values in the data set (with the exception of *MRL¹* values that are too
368 low to allow all animals to arrive at a safe concentration at the last time point).

369 A monotonic regression is applied to the resulting set of (*MRL¹*,*UWP*) pairs. If the *UWP* values are
370 arranged according to increasing *MRL¹* values using an index *j*, then the fitted values from monotonic
371 regression (*MUWP_j*) are calculated by iterated weighted averaging of pairs where *UWP* increases with
372 *MRL¹*. Start with *MUWP_j*=*UWP_j* and weights *w_j*=1, for all *j*. Then, for any adjacent pair (*j*,*j*+1) with
373 *MUWP_j*<*MUWP_{j+1}*, replace the pair by one value, the weighted average

$$374 \quad (w_j MUWP_j + w_{j+1} MUWP_{j+1}) / (w_j + w_{j+1})$$

375 and set the new weight equal to *w_j*+*w_{j+1}*. Repeat this procedure until the resulting averages satisfy the
376 imposed negative relation between *MRL¹* and *MUWP*. The resulting weighted averages are valid for all
377 underlying *MRL¹* values.

378 *Step 10. Calculate withdrawal period*

379 Finally, the *MUWP* value corresponding to the real *MRL¹* is rounded upward to an integer number of
380 milkings. This should be converted to the withdrawal period in real time.

$$381 \quad WP = (\Delta t) \text{ int } (MUWP + 1)$$

382 where Δt is the interval in hours between milkings in the experiments (e.g. 12 hours).

383 See Annex II for an example of the application of this procedure.

384

385 **Annex I: Comparison of several approaches for establishing** 386 **milk withdrawal periods**

387 ***I.1 Introduction***

388 The point of departure was to examine the linear regression method developed by the US Food and Drug
389 Administration (FDA) for its suitability to be used in the EU. However, as this method had certain
390 characteristics which made it difficult to be applied in the European situation (in the European situation
391 e.g. withdrawal periods are established for individual animals, the data sets are often not suited for linear
392 regression, and usually no data are available on intra-individual variability), and because developments
393 in statistical science should be taken into account, a modification of the FDA method and alternatives for
394 this method were investigated. The FEDESA ad hoc Working Party on Harmonisation of Withdrawal
395 Periods provided useful additional information with regard to suitable alternatives and data sets to test
396 the different methods.

397 The methods were applied to eleven real data sets (not shown here due to confidentiality), and the
398 results were evaluated to select the most appropriate method. The results were compared with each
399 other and with results achieved by applying two so-called "simple" methods as used previously in
400 different Member States (i.e., first milking with all concentrations below MRL¹, and the first milking with
401 all concentrations below MRL¹ plus a "safety span". A detailed description of these methods lies beyond
402 the scope of this Note for Guidance).

403 ***I.2 SCLR method: Safe concentrations, based on linear regression, and*** 404 ***allowing for measurements below the limit of quantification (LOQ)***

405 This is a modification of the FDA method [8,14]. In principle the method fits a regression line to the log
406 concentration data of each cow. The fitted lines are used to estimate the distribution of log concentrations
407 at each time point. Estimates are made of between-animal variance and of measurement error variability,
408 and these are then used to calculate a log concentration tolerance limit at each time point. The estimated
409 withdrawal period is the first time point where the tolerance limit is at or below the MRL¹. Referral is
410 made to the FDA guideline for computational details.

411 The method used here deviates from the FDA method on the following points:

- 412 • Calculation of 95% tolerance limits (FDA chooses 99% tolerance limits)
- 413 • All animals used in the withdrawal time calculation are assumed to have been treated (FDA assumes
414 that if the product is used to treat mastitis, no more than one-third of the milk comes from treated
415 animals).
- 416 • No requirement for the number of animals (FDA requires at least 20 animals).
- 417 • No requirement for the number of replicate analyses per milk samples (FDA requires triplicate
418 assays). When no replicate measurements were available an external estimate of assay variance was
419 used.
- 420 • Regression lines are calculated by maximising the combined normal likelihood of values at or above
421 the LOQ and measurements reported as 'below the LOQ' (FDA excludes the latter measurements as
422 well as other data from time points with less than three remaining values). The likelihood to be
423 optimised has the form

$$424 \prod_{i \in A} (2\pi\sigma^2)^{-1/2} \exp\left\{-\frac{(y_i - \beta_0 - \beta_1 t)^2}{\sigma^2}\right\} \prod_{i \in B} \Phi\left\{\frac{(y_{LOQ} - \beta_0 - \beta_1 t)}{\sigma}\right\}$$

425 where y_i is the log concentration of animal/time combination i , y_{LOQ} is the natural logarithm of the
426 LOQ, A is the set of values $\{i; y_i \geq y_{LOQ}\}$ and B is the set of censored values $\{i; y_i < y_{LOQ}\}$. β_0 and β_1 are
427 the regression line slope and intercept, and σ is the residual standard error. Φ denotes the cumulative
428 standard normal distribution.

- 429 • No checks on log-linearity (FDA prescribes lack-of-fit F tests per animal to select points to be used for
430 subsequent calculations).

431 **I.3 SCPM method: Safe concentrations, based on data per milking, allowing** 432 **for data below the limit of quantification**

433 This approach is similar to the approach described in [15]. Essentially, a tolerance limit is calculated from
434 the measured values at each time point separately. A normal distribution is assumed for the log
435 concentrations. Allowance for data below the LOQ is made by using a maximum likelihood method.

436 In some cases a shorter withdrawal period can be obtained by a pre-processing step termed monotonic
437 regression. This least squares procedure replaces the data values of each cow by fitted values under the
438 only condition that these fitted values should be non-increasing with time.

439 The tolerance limit is calculated as

$$440 y_{tol} = \hat{\mu} + k \hat{\sigma}$$

$$441 k = t_{v, \delta, \alpha} / \sqrt{n}$$

$$442 v = n - 1$$

$$443 \delta = z_p \sqrt{(n/m)}$$

444 where n is the number of cows observed and m is the number of cows contributing milk to a bulk tank, z_p
445 is the 100th percentile point of the standard normal distribution (e.g. $z_{0.95} = 1.645$), and $t_{v, \delta, \alpha}$ is the
446 100(1- α)th percentile of the non-central t distribution with v degrees of freedom and non-centrality

447 parameter δ . $\hat{\mu}$ and $\hat{\sigma}$ are estimates of the mean and standard deviation of the normal distribution at
448 this time point. For uncensored data these are just the usual mean and sample standard deviation

449 calculated from the data. With some of the data below the LOQ the estimates $\hat{\mu}$ and $\hat{\sigma}$ are made by
450 maximising the likelihood

$$451 \prod_{i \in A} (2\pi\sigma^2)^{-1/2} \exp\{-(y_i - \mu)^2 / \sigma^2\} \prod_{i \in B} \Phi\{(y_{LOQ} - \mu) / \sigma\}$$

452 where y_i is the log concentration of animal i , y_{LOQ} is the natural logarithm of the LOQ, A is the set of
453 values $\{i; y_i \geq y_{LOQ}\}$ and B is the set of censored values $\{i; y_i < y_{LOQ}\}$. μ and σ are the mean and the
454 standard error. Φ denotes the cumulative standard normal distribution.

455 The withdrawal period is the first time point where $y_{tol} \leq y_{MRL}$, and where this condition is not violated at
456 later time points in the data set.

457 Some complications involving the censored values arise a) with replicate measurements; b) when
458 monotonic regression is used as a pre-processing step.

459 When replicate measurements (per milk sample) are available, a first step is to take the mean of the log
460 concentration values. Also the monotonic regression procedure requires the calculation of (weighted)
461 means of log concentration values across two or more time points whenever the data are increasing with
462 time. How should censored values be treated when calculating these means? As a conservative approach,
463 censored data are set equal to y_{LOQ} . Any value remaining equal to y_{LOQ} after these two pre-processing
464 steps is reset to a censored observation (set B) in the ML method.

465 When at any time point all observations are censored, the theoretical maximum likelihood estimate of log
466 concentration is $-\infty$. However, in the program used for this study, the optimisation program left the
467 estimate at its initial value. The standard deviation of the log concentration distribution was set, quite
468 arbitrarily, to the smallest non-zero standard deviation in the original data set (which was the data set
469 with censored values entered arbitrarily as LOQ).

470 **I.4 TTSC method: Based on times-to-safe-concentration**

471 This is the approach described as the harmonised approach in the main document of this Note for
472 Guidance (chapter 2.2).

473 **I.5 Discussion of results**

474 **I.5.1 Safe concentration from linear regression (SCLR) approach**

475 **I.5.1.1 Linearity**

476 The main characteristic of the SCLR approach is the assumption of a linear relation between log
477 concentration and time. If this assumption is sufficiently close to the truth then linear regression gives
478 the most accurate estimates of log concentration at any time point or of the time to reach a safe
479 concentration for each cow.

480 However, the assumption of linearity may fail for the following reasons:

481 1. There may be need for two (or more) pharmacokinetic compartments in an appropriate model,
482 implying that concentration should be modelled as a sum of exponentials. Although such a model
483 could be fitted in principle, in practice the data are often too scarce to allow a proper choice between
484 one- or more-component models, or even to fit a more-component model.

485 The practical alternative advocated by the FDA [8] is to use only points in the final linear phase of the
486 depletion curves. Lack-of-fit F tests may be used to decide which points to exclude. For these tests an
487 estimate of 'pure error' variance is needed, either from replicated assays [8] or as external
488 information to be supplied by the applicant.

489 2. Binding of the substance to e.g. plasma proteins may be relatively higher at low concentrations. This
490 may cause upward deviations from the final log concentration depletion line.

491 3. Circadian (or other) biorhythms may cause cyclic deviations from the values predicted by the linear
492 depletion model.

493 Deleting points to achieve linearity may be sensible in case 1, but does not seem to provide a solution in
494 cases 2 and 3.

495 Of course, in practice deviations from linearity may be small enough to ignore them.

496 **I.5.1.2 Data below the limit of quantification**

497 There are two problems with the SCLR approach when there are data below the LOQ (known in statistics
498 as censored data):

499 1. Fitting the regression lines.

500 Simple approaches are replacement of censored data with 0, $\frac{1}{2}$ LOQ, or LOQ, or deletion of time
501 points with data $<$ LOQ. The latter approach is advocated in the FDA method. Such methods have no

502 theoretical basis, and have been found to perform poorly in many studies (see e.g. [16] and
503 references therein).

504 Maximum likelihood estimation (MLE) is a general statistical technique, which can also be used for
505 estimating regression functions in the presence of censored data (see e.g. [17,18]). The application of
506 MLE requires the optimisation of a non-linear function, which is easily performed by standard
507 statistical programs. According to [16] MLE methods are commonly used in environmental disciplines
508 such as air quality studies and geochemistry.

509 Users of MLE methods should be warned that the theory behind MLE is based on large samples.
510 Therefore, data sets should not be too small: for small sample sizes ($n=5, 10, 15$) estimates may
511 have large bias and poor precision [16]. The ML estimate of the residual variance (needed in the
512 tolerance limit calculations) will be badly biased when the number of uncensored observations is small
513 [17].

514 2. Estimating the inter animal variability

515 At each time point the data show animal variability and assay variability, where the former is often
516 much larger than the latter. In the SCLR approach between animal variability will be estimated from
517 the fitted values at that time point. When all animals have measurements above the LOQ this is a
518 reasonable procedure. However, with many data below the LOQ, one may obtain a widely diverging
519 bundle of regression lines on the log concentration scale. It then occurs that at a certain time point all
520 fitted values are below the LOQ, but they are widely different, ranging over e.g. a factor 1000 for the
521 ratio of concentrations. In the subsequent tolerance calculations the large inter animal variance will
522 make it impossible to guarantee that 95 % of the population is below MRL¹. Essentially, the SCLR
523 approach requires that the linearity assumption is accepted for all unobserved values below the LOQ,
524 and that no upper limit is put on the (partly or wholly unobserved) inter animal variability of the log
525 concentrations.

526 **I.5.2 Safe concentration per milking (SCPM) approach**

527 The advantage of the SCPM approach over the SCLR approach is that no linearity needs to be assumed in
528 cases where this seems questionable. Therefore, problems regarding the linearity lack-of-fit tests and any
529 artificially enlarged inter animal variability, if many data are below the LOQ, are avoided. Another
530 advantage is that the variance at each time point is allowed to be different.

531 The disadvantage is that information is not optimally used whenever linearity and homogeneity of
532 variance are valid assumptions, especially if the number of animals is small. Moreover, extrapolation
533 beyond the range of observed time points in the experiment is impossible.

534 An intermediate approach between linear regression and pure per-milking is the use of monotonic
535 regression (also termed isotonic regression, see [10]). In this note the use of monotonic regression is
536 considered as a variation of the PM approach. In monotonic regression, data points that contradict the
537 prior assumption of concentration decreasing with time are replaced by weighted averages of data points.
538 Technically, the data points y_{ij} of a cow i (averaged over replicated analyses if appropriate) are replaced
539 by fitted values equal to $\min_{s \leq j} \max_{t \geq j} A_v(s,t)$, where $A_v(s,t)$ is the average value of $y_{is}, y_{i(s+1)}, \dots, y_{it}$. In
540 practice most values are left unaltered, with only those few that show an increasing instead of decreasing
541 trend being replaced by averages. Nevertheless, the influence on the estimated withdrawal period may
542 be large.

543 Handling data below the LOQ may be more difficult with the SCPM approach as compared to the SCLR
544 approach. Technically the MLE procedure is almost the same, but the number of uncensored observations

545 is in most cases much smaller than with the SCLR approach. Consequently, the ML estimates of standard
546 errors and tolerance limits may be very biased.

547 **I.5.3 Time-to-safe-concentration (TTSC) approach**

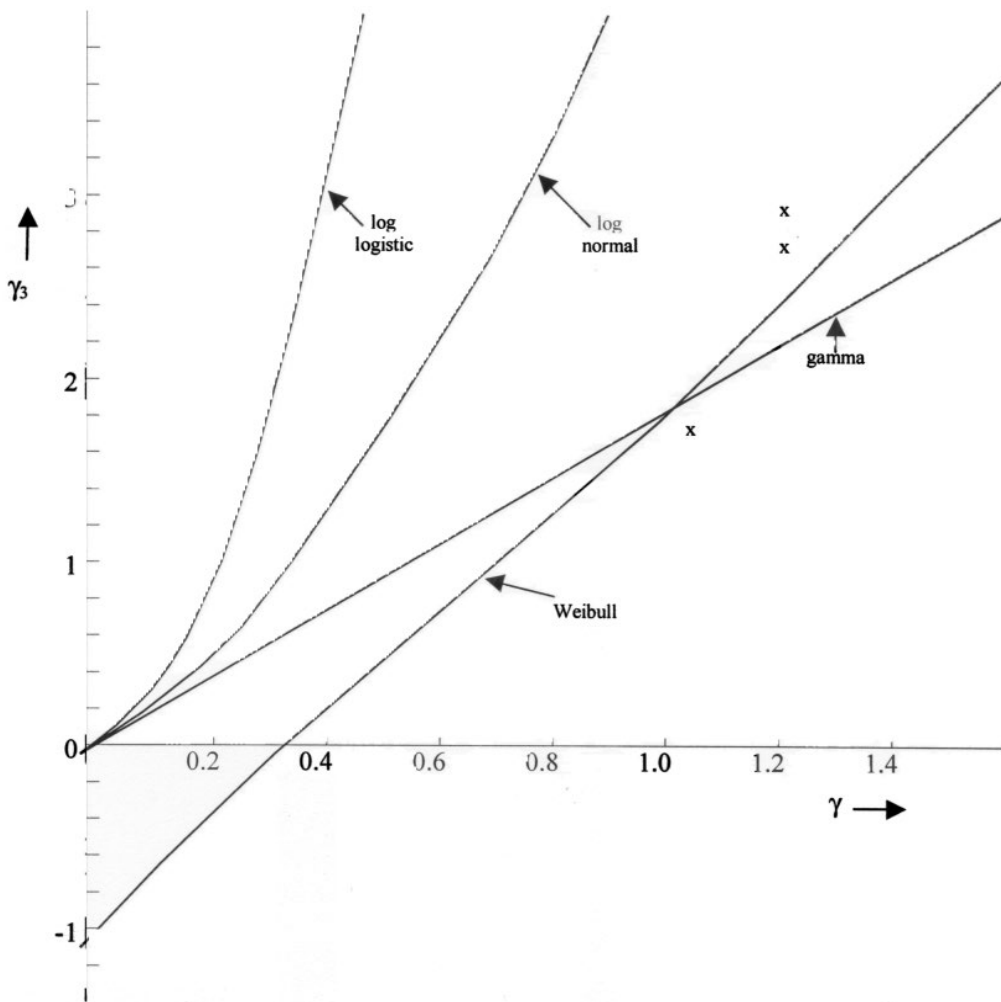
548 The TTSC approach has the same advantage as the SCPM approach: no assumption of linear depletion is
549 needed. Moreover, there are in principle no problems with data below the LOQ: a data point below the
550 LOQ just counts as a point below MRL¹. Therefore, there is no need for the MLE approach with its
551 uncertain behaviour in small samples.

552 A disadvantage of the TTSC approach is that we need a distributional assumption for the TTSC values.
553 Whereas standard theory supports the assumption of log-normality for concentrations, no such theory
554 exists for the times necessary to reach a safe concentration. In practice, therefore, we need an empirical
555 choice for a distribution, which fits the data well enough. A further problem is that the TTSC values per
556 animal are discrete (milkings), whereas proposed distributions (normal, log-normal, Weibull) are defined
557 for continuous variables. Treating a discrete variable as if it were a continuous variable may lead to
558 withdrawal period estimates, which are too short.

559 A comparison has been made between several distributional assumptions. 95 % tolerance limits are
560 statements about the 95 % percentile of the population. Therefore, large differences are expected when
561 distributions with the same mean and variance, but different skewness are fitted to some data. Based on
562 the linear regression model it is expected that TTSC values will show a right-skewed distribution, and this
563 is indeed almost always true. Normal-theory tolerance limits may therefore be expected to be too low.

564 Chester et al. (2) propose to use tolerance limit calculations based on a normal distribution anyway. They
565 investigated the performance in the case of normal and non-normal distributions using Monte Carlo
566 simulations from continuous g-and-h distributions [19]. They simulated TTSC values with 95 %
567 percentiles of 5.50, 5.75, 6.00 and 6.25 (milkings), and concluded that the 95 % tolerance limit provided
568 at least 95 % confidence for all but the most skewed distributions ($g=0.6$, $h=0.3$), when the target 95 %
569 percentile was 6.25. It may be concluded that in these simulations, where withdrawal period was
570 considered as a continuous variable, the downward bias from using normal-theory calculations was
571 compensated in most cases by the upward bias from using TTSC values rounded upward to whole
572 milkings. It is unclear whether this would also be the case with simulations from a discrete distribution,
573 or in cases where the withdrawal period is a larger multiple of 12 hours milking periods (so that rounding
574 effects are relatively small).

575 Figure:

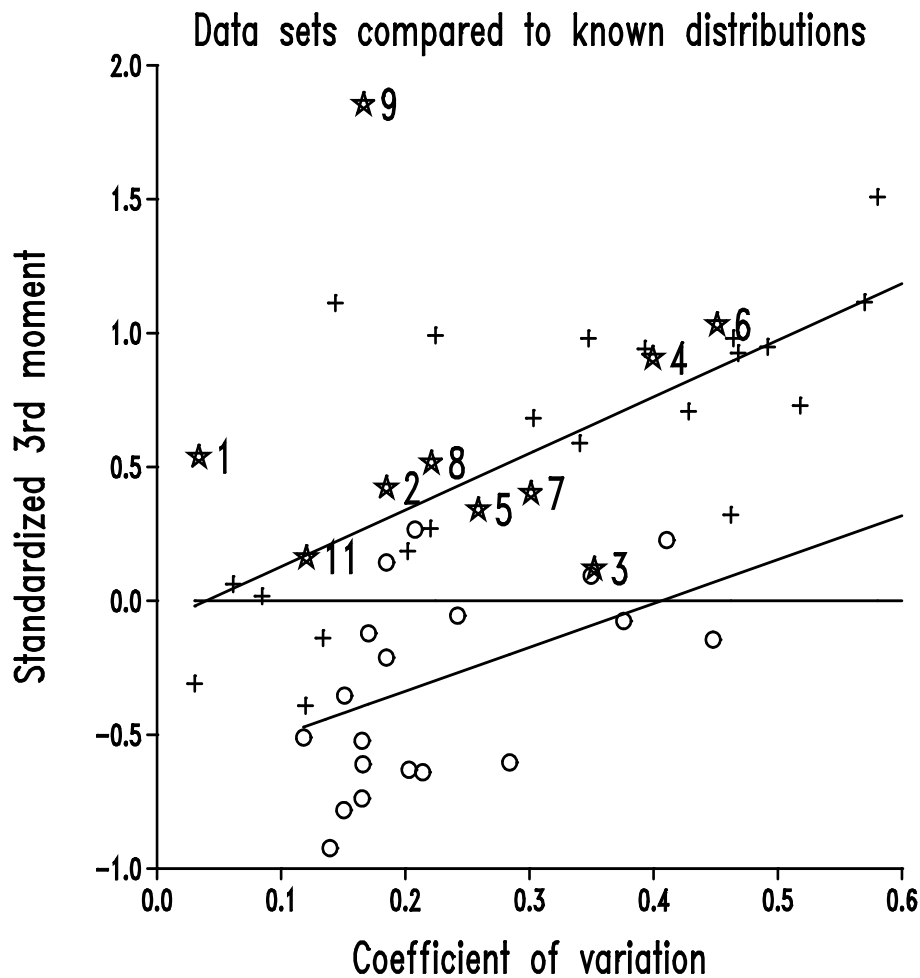


576

577 Figure 1. Standardised third moment, γ_3 , vs. coefficient of variation, γ for log logistic, log-normal,
578 gamma and Weibull distributions. Exponential distribution is at point (1,2). Reproduced from
579 [20].

580 For several standard distributions (log-normal, log-logistic, gamma, Weibull) the skewness is a function
581 of the coefficient of variation only (see Figure 1 reproduced from [20]). In general the skewness,
582 expressed as the standardised third moment $\gamma_3 = \mu_3/s^3$, increases with the coefficient of variation $\gamma = \sigma/\mu$. A
583 high value of γ_3 implies a relatively long right tail. At a certain coefficient of variation the tail of the log-
584 logistic distribution is longer than that of a log-normal distribution, which in turn is longer than the tail of
585 a gamma distribution. It is noteworthy that the Weibull distribution is actually skewed to the left instead
586 of to the right for coefficients of variation less than approximately 30 %. A practical advantage of the log-
587 normal distribution is that calculations remain just as simple as in the case of a normal distribution: one
588 simply works with $\ln(\text{TTSC})$ instead of TTSC values.

589 In an empirical evaluation on real data sets the distributional assumption made a difference for the
590 established withdrawal period in most of the data sets. The pattern always was: increasing withdrawal
591 periods in the order Weibull, normal, log-normal. This is in accordance with theory. Figure 2 shows the
592 position of 11 real data sets in the plot of standardised third moment against coefficient of variation,
593 together with points for data sets of size $n=25$ simulated from Weibull or log-normal distributions. The
594 normal distribution (simulations not shown) gives points around a horizontal line with standardised third
595 moment 0 (symmetric distribution).



596

597 Figure 2. Skewness against variability for data sets (stars) and simulations from log-normal (crosses
 598 and upper regression line) and Weibull (circles and lower regression line) distributions.

599 It can be seen that most data sets are more like simulations from a log-normal distribution than from a
 600 Weibull distribution. The most deviating data sets are 1, 3 and 9. Data set 1 is a set with just n=6 cows.
 601 Data sets 9 and 3 are cases with a short withdrawal period and therefore a large distortion from rounding
 602 to integer values.

603

604 **Annex II: Example of the TTSC approach**

605 Figure 3 and Table 2 show data for $n = 25$ animals and 8 milkings (in a 12-hours milking scheme, with
606 the last treatment 12 hours before the first milking). These artificial data were generated by simulation
607 based on a real data set. In the simulation normal error was added to linear regression estimates of the
608 log concentration values in a real data set.

609 Monotonic regression pre-processing was applied to the example data (see Table 3). Consider for
610 example the data and graph for cow 1, where the log concentrations of milkings 2 and 3 were averaged
611 ($\ln(0.402)$ is the average of $\ln(0.341)$ and $\ln(0.473)$), as well as the log concentrations of milkings 4, 5
612 and 6.

613 The MRL in this example is 0.1. At the last milking, all cows have a (pre-processed) value not higher than
614 MRL, therefore the TTSC method can be applied. TTSC values per cow are now calculated, and
615 summarised in Table 4.

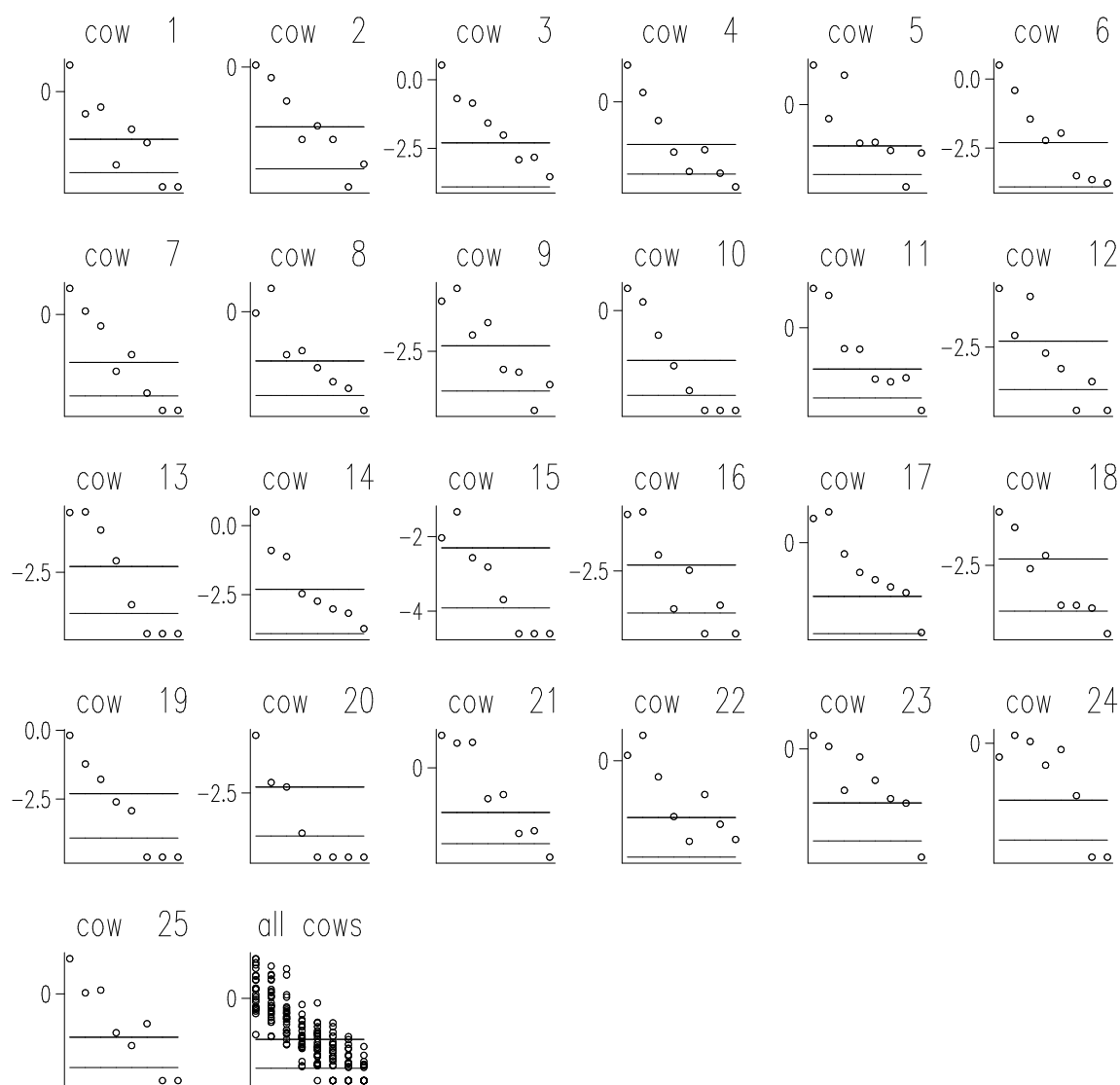
616 The mean m and standard deviation s of the $\ln(\text{TTSC})$ values are 1.556 and 0.2779, respectively. With a
617 tolerance limit factor $k = 2.292$ (see Table 1) this leads to a 95/95 tolerance limit of $1.556 + 2.292 \cdot 0.2779$
618 $= 2.193$ on the logarithmic scale, corresponding to $e^{2.193} = 8.962$ on the milking interval scale.

619 If the TTSC method would be applied without the last monotonic regression step, the tolerance limit
620 8.962 would be rounded upward to obtain a withdrawal period of 9 milking intervals, or $9 \times 12 = 108$ hours.

621 In the last monotonic regression step of the TTSC method the calculations above are repeated with MRL
622 values chosen over the range of the data. In practice MRL values are chosen equal to all concentration
623 values where at least one of the TTSC values changes. The resulting set of (MRL,UWP)-pairs is shown in
624 Table 5 and Figure 4, together with fitted UWP values after applying monotonic regression. At the true
625 MRL of 0.1 the fitted UWP is slightly lower, 8.886 instead of 8.962. In this example the resulting
626 withdrawal period of 9 milking intervals is unaltered.

627 The stabilising effect of the last monotonic regression step can be illustrated by noting the effect on
628 withdrawal period of changes in MRL. For a real MRL of 0.15 the withdrawal period would remain 9
629 (instead of 8) milking intervals, for a real MRL of 0.20 it would still be 9 (instead of 10) milking intervals.

630 Thus, the withdrawal period is fixed at $9 \times 12 = 108$ hours. Milk from milkings at or after 108 hours after
631 treatment is considered safe. With a regular 12-hours milking scheme the first safe milk is milk from the
632 9th milking if treatment in practice is given 12 hours before the first milking, and milk from the 10th
633 milking if treatment is given less than 12 hours before the first milking.



634

635

636

Figure 3. Example data (simulated). Log concentration vs. time (milking). Horizontal lines mark MRL=0.1 and LOQ=0.02. Data <LOQ are shown at LOQ.

Table 2. Example data set. 25 animal (rows) and 8 time points (columns). MRL=0.1 and LOQ=0.02. Data below LOQ were entered as 0.01.

3.609	0.341	0.473	0.029	0.162	0.085	0.010	0.010
1.077	0.665	0.270	0.062	0.104	0.062	0.010	0.024
1.714	0.503	0.426	0.206	0.133	0.054	0.059	0.029
7.342	1.656	0.362	0.066	0.023	0.075	0.021	0.010
9.201	0.454	5.220	0.116	0.122	0.077	0.010	0.067
1.662	0.663	0.234	0.108	0.141	0.030	0.026	0.023
3.482	1.176	0.576	0.065	0.145	0.023	0.010	0.010
0.942	2.961	0.134	0.162	0.073	0.038	0.028	0.010
0.492	0.774	0.147	0.229	0.043	0.039	0.010	0.025
2.766	1.483	0.320	0.078	0.025	0.010	0.010	0.010
8.963	6.073	0.311	0.303	0.057	0.049	0.061	0.010
0.577	0.121	0.442	0.067	0.040	0.010	0.026	0.010
0.635	0.649	0.348	0.122	0.027	0.010	0.010	0.010
1.646	0.408	0.327	0.085	0.065	0.049	0.042	0.024

Table 2. Example data set. 25 animal (rows) and 8 time points (columns). MRL=0.1 and LOQ=0.02. Data below LOQ were entered as 0.01.

0.131	0.263	0.077	0.060	0.025	0.010	0.010	0.010
0.545	0.593	0.140	0.023	0.084	0.010	0.026	0.010
2.848	3.779	0.619	0.280	0.204	0.150	0.117	0.021
0.425	0.263	0.074	0.111	0.024	0.024	0.022	0.010
0.832	0.294	0.168	0.074	0.054	0.010	0.010	0.010
0.547	0.116	0.100	0.022	0.010	0.010	0.010	0.010
5.333	3.578	3.717	0.203	0.251	0.034	0.039	0.010
1.242	2.800	0.518	0.104	0.038	0.253	0.076	0.041
1.780	1.110	0.171	0.708	0.262	0.120	0.099	0.010
0.573	1.380	1.075	0.412	0.776	0.120	0.010	0.010
6.483	1.060	1.225	0.127	0.064	0.205	0.010	0.010

637

Table 3. Example data from Table 2 pre-processed by monotonic regression against time.

3.609	0.402	0.402	0.074	0.074	0.074	0.020	0.020
1.077	0.665	0.270	0.080	0.080	0.062	0.022	0.022
1.714	0.503	0.426	0.206	0.133	0.056	0.056	0.029
7.342	1.656	0.362	0.066	0.042	0.042	0.021	0.020
9.201	1.539	1.539	0.119	0.119	0.077	0.037	0.037
1.662	0.663	0.234	0.123	0.123	0.030	0.026	0.023
3.482	1.176	0.576	0.097	0.097	0.023	0.020	0.020
1.670	1.670	0.147	0.147	0.073	0.038	0.028	0.020
0.617	0.617	0.183	0.183	0.043	0.039	0.022	0.022
2.766	1.483	0.320	0.078	0.025	0.020	0.020	0.020
8.963	6.073	0.311	0.303	0.057	0.055	0.055	0.020
0.577	0.231	0.231	0.067	0.040	0.023	0.023	0.020
0.642	0.642	0.348	0.122	0.027	0.020	0.020	0.020
1.646	0.408	0.327	0.085	0.065	0.049	0.042	0.024
0.186	0.186	0.077	0.060	0.025	0.020	0.020	0.020
0.568	0.568	0.140	0.044	0.044	0.023	0.023	0.020
3.281	3.281	0.619	0.280	0.204	0.150	0.117	0.021
0.425	0.263	0.091	0.091	0.024	0.024	0.022	0.020
0.832	0.294	0.168	0.074	0.054	0.020	0.020	0.020
0.547	0.116	0.100	0.022	0.020	0.020	0.020	0.020
5.333	3.647	3.647	0.226	0.226	0.036	0.036	0.020
1.865	1.865	0.518	0.104	0.098	0.098	0.076	0.041
1.780	1.110	0.348	0.348	0.262	0.120	0.099	0.020
0.947	0.947	0.947	0.565	0.565	0.120	0.020	0.020
6.483	1.140	1.140	0.127	0.115	0.115	0.020	0.020

638

Table 4. Time to safe concentration (TTSC) values per cow.

TTSC	ln(TTSC)	frequency	cow numbers
3	1.099	3 ***	15, 18, 20
4	1.386	9 *****	1, 2, 4, 7, 10, 12, 14, 16, 19
5	1.609	5 *****	8, 9, 11, 13, 22
6	1.792	4 ****	3, 5, 6, 21
7	1.946	3 ***	23, 24, 25
8	2.079	1 *	17

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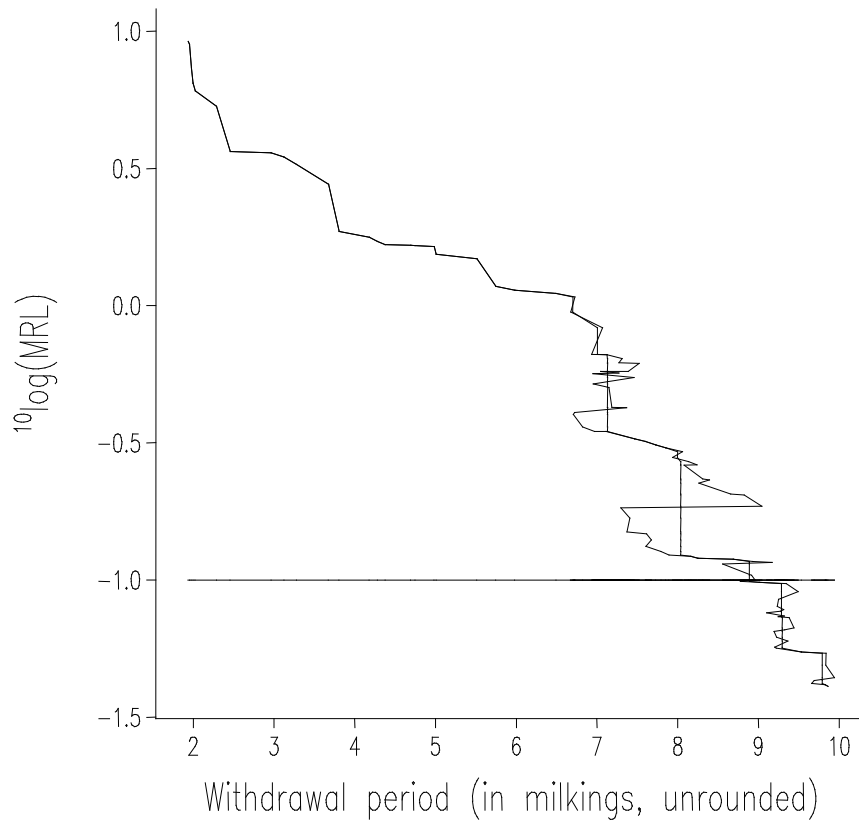
Table 5. Un-rounded withdrawal period (UWP) and monotonic fit (MUWP) at varying MRL values. UWP and MUWP values are valid from the tabulated MRL up to the next tabulated MRL value, e.g. MRL=0.20 gives UWP=9.044 and MUWP=8.035.

MRL	UWP	MUWP	MRL	UWP	MUWP
0.0410	9.861	9.861	0.2800	7.937	7.997
0.0415	9.826	9.826	0.2940	8.057	7.997
0.0420	9.657	9.792	0.3030	7.852	7.852
0.0430	9.692	9.792	0.3110	7.728	7.728
0.0440	9.942	9.792	0.3200	7.599	7.599
0.0490	9.834	9.792	0.3270	7.467	7.467
0.0540	9.836	9.792	0.3479	7.114	7.130
0.0547	9.534	9.534	0.3480	6.970	7.130
0.0564	9.219	9.293	0.3620	6.823	7.130
0.0570	9.201	9.293	0.4016	6.706	7.130
0.0600	9.364	9.293	0.4080	6.725	7.130
0.0620	9.228	9.293	0.4250	7.367	7.130
0.0650	9.191	9.293	0.4260	7.182	7.130
0.0660	9.323	9.293	0.5030	7.148	7.130
0.0670	9.440	9.293	0.5180	6.955	7.130
0.0730	9.381	9.293	0.5470	7.460	7.130
0.0736	9.246	9.285	0.5654	6.948	7.130
0.0740	9.319	9.285	0.5685	7.272	7.130
0.0760	9.104	9.285	0.5760	7.047	7.130
0.0770	9.272	9.285	0.5770	7.388	7.130
0.0780	9.311	9.285	0.6171	7.524	7.130
0.0803	9.232	9.285	0.6190	7.273	7.130
0.0850	9.248	9.285	0.6420	7.312	7.130
0.0906	9.490	9.285	0.6630	7.126	7.126
0.0971	9.345	9.285	0.6650	6.935	7.003
0.0981	9.011	9.011	0.8320	7.071	7.003
0.0990	8.777	8.886	0.9473	6.675	6.702
0.1000	8.962	8.886	1.0770	6.728	6.702
0.1040	8.919	8.886	1.1100	6.494	6.494
0.1145	8.558	8.886	1.1395	5.982	5.982
0.1160	9.170	8.886	1.1760	5.748	5.748
0.1170	8.930	8.886	1.4830	5.513	5.513
0.1190	8.688	8.688	1.5394	5.010	5.010
0.1200	8.249	8.249	1.6460	4.985	4.985
0.1220	8.164	8.164	1.6560	4.746	4.746
0.1234	7.892	8.035	1.6620	4.694	4.694
0.1270	7.794	8.035	1.6701	4.376	4.376
0.1330	7.607	8.035	1.7140	4.285	4.285
0.1400	7.675	8.035	1.7800	4.181	4.181
0.1473	7.612	8.035	1.8648	3.807	3.807
0.1500	7.373	8.035	2.7660	3.675	3.675
0.1680	7.409	8.035	3.2806	3.277	3.277
0.1835	7.297	8.035	3.4820	3.125	3.125
0.1856	9.044	8.035	3.6090	2.965	2.965
0.2040	8.824	8.035	3.6468	2.457	2.457
0.2060	8.655	8.035	5.3330	2.289	2.289
0.2257	8.261	8.035	6.0730	2.024	2.024
0.2313	8.395	8.035	6.4830	1.998	1.998

MRL	UWP	MUWP
0.2340	8.311	8.035
0.2620	8.079	8.035
0.2630	8.238	8.035
0.2700	8.135	8.035

MRL	UWP	MUWP
7.3420	1.976	1.976
8.9630	1.957	1.957
9.2010	1.938	1.938

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646 Figure 4. Effect of final monotonic regression to obtain monotonically increasing withdrawal periods for
 647 decreasing MRLs. Vertical line segments are monotonic fits *MUWP* replacing calculated *UWP*
 648 *values*. Horizontal line indicates the true $MRL=0.1$ for this example, and intersects the *MUWP*
 649 curve at 8.886, which upon rounding gives a withdrawal period (*WP*) of 9 milkings.

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